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# Numerical Simulations of Turbulent Flow in Pipes

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# Motivation

- Particle-Laden flow in industrial application
  - Complex Geometries
  - Erosion
- Geometries of focus
  - Elbow
  - Plugged T-junction
- Computational Method
  - Reynolds averaged Navier-Stokes (RANS)
  - Direct Numerical Simulation (DNS)
  - Lagrangian particle tracking (LPT)



# Objective

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## Overall objectives

- Conduct high fidelity numerical simulations for detailed insight into the physics of erosion
- Validate simulations with experimental data
- Enhance RANS methods

## Current objectives

- Determine ideal turbulence model
- Present DNS duct data (Validation)
- Present coarse DNS elbow data

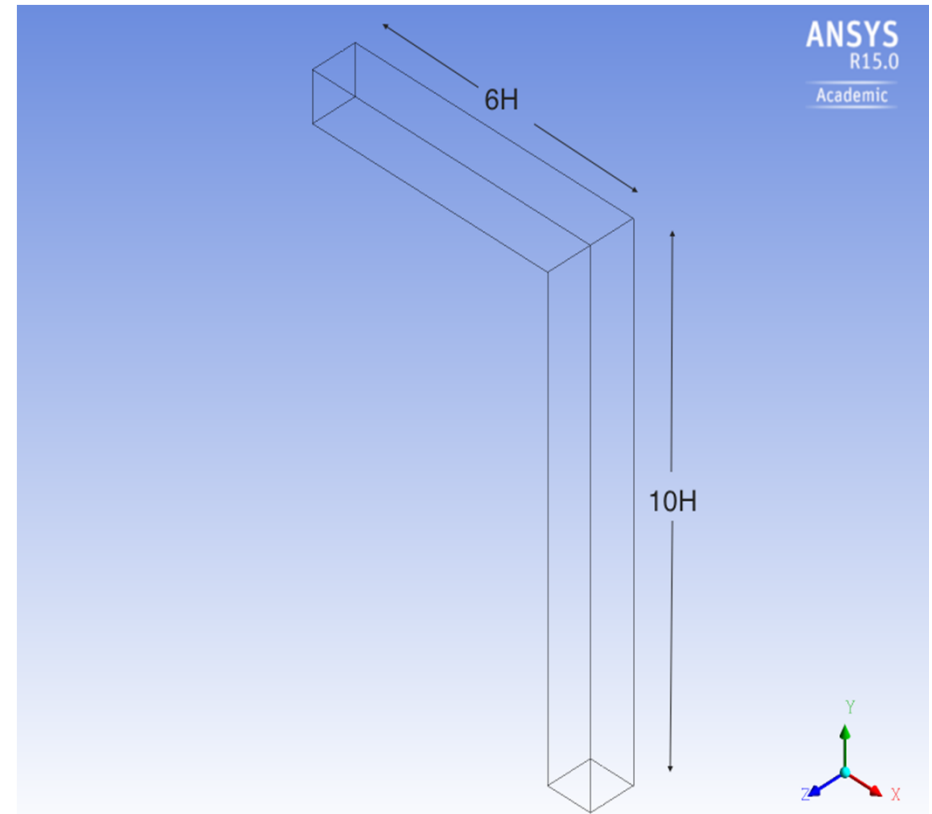
# Reynolds Averaged Navier-Stokes (RANS)

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- Navier-Stokes decomposed into mean and fluctuating terms
- Closure problem
- k- $\epsilon$  model
  - Two equation model
  - Assumes that the viscosity is isotropic
- Reynolds stress model (RSM)
  - Solves for the Reynolds terms directly
  - Computational expense higher than other RANS models

# Reynolds Averaged Navier-Stokes (RANS)

- Cross-section of geometries square
- $Re=11,500-115,000$
- Entrance and exit length
- Boundary conditions
- Enhanced wall treatment
- 2-4 million elements



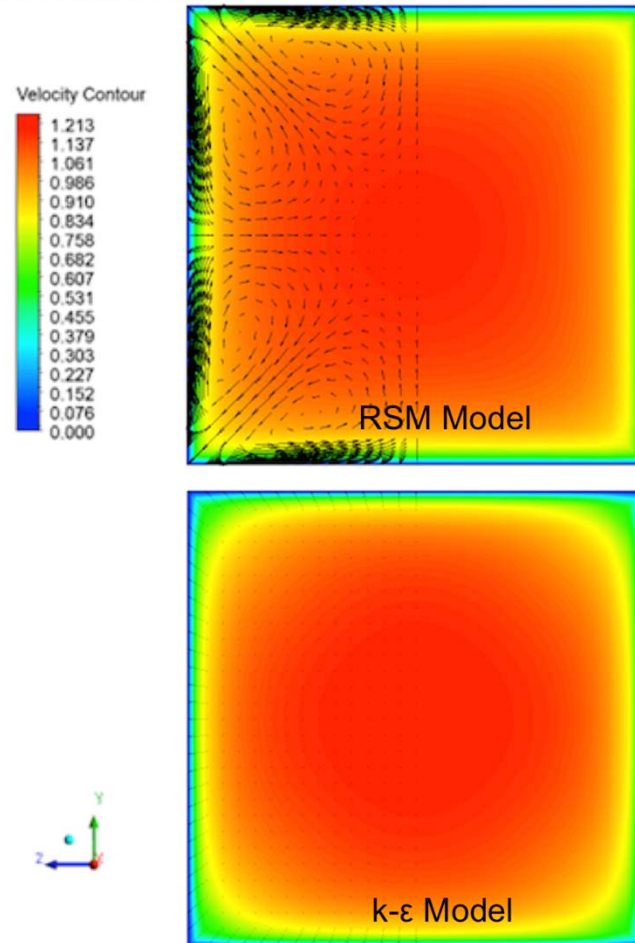
# Reynolds Averaged Navier-Stokes (RANS)

## Model comparison

- Upstream of bend
- $Re = 11,500$
- Streamwise velocity contours overlaid with secondary flow vectors

## Observation

- $k-\epsilon$  model does not show secondary flow vectors
- The secondary motion directs the flow into the corners making the flow more uniform

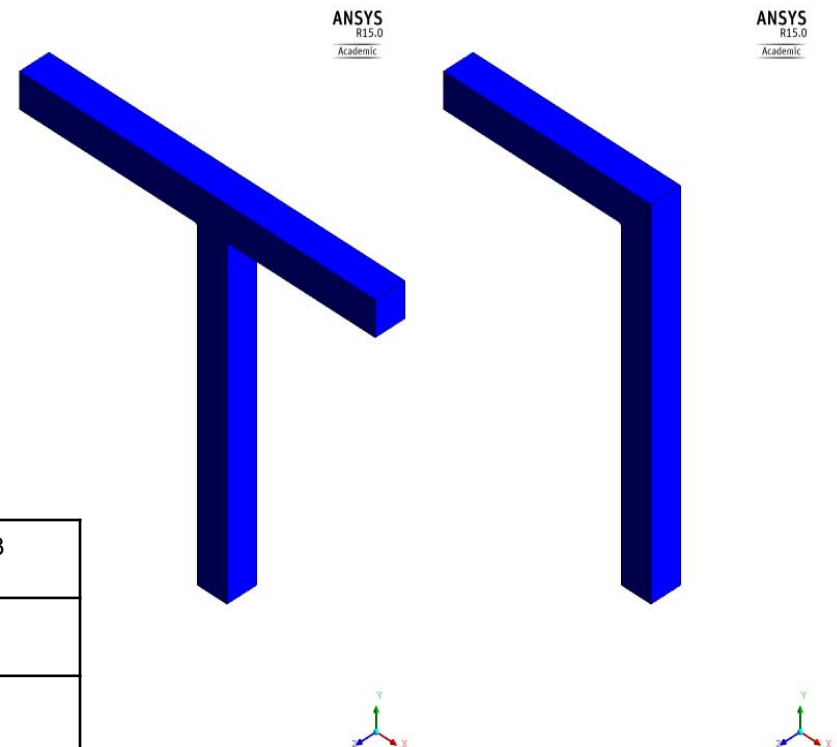


# RANS RSM model

## Particle-Laden Flow

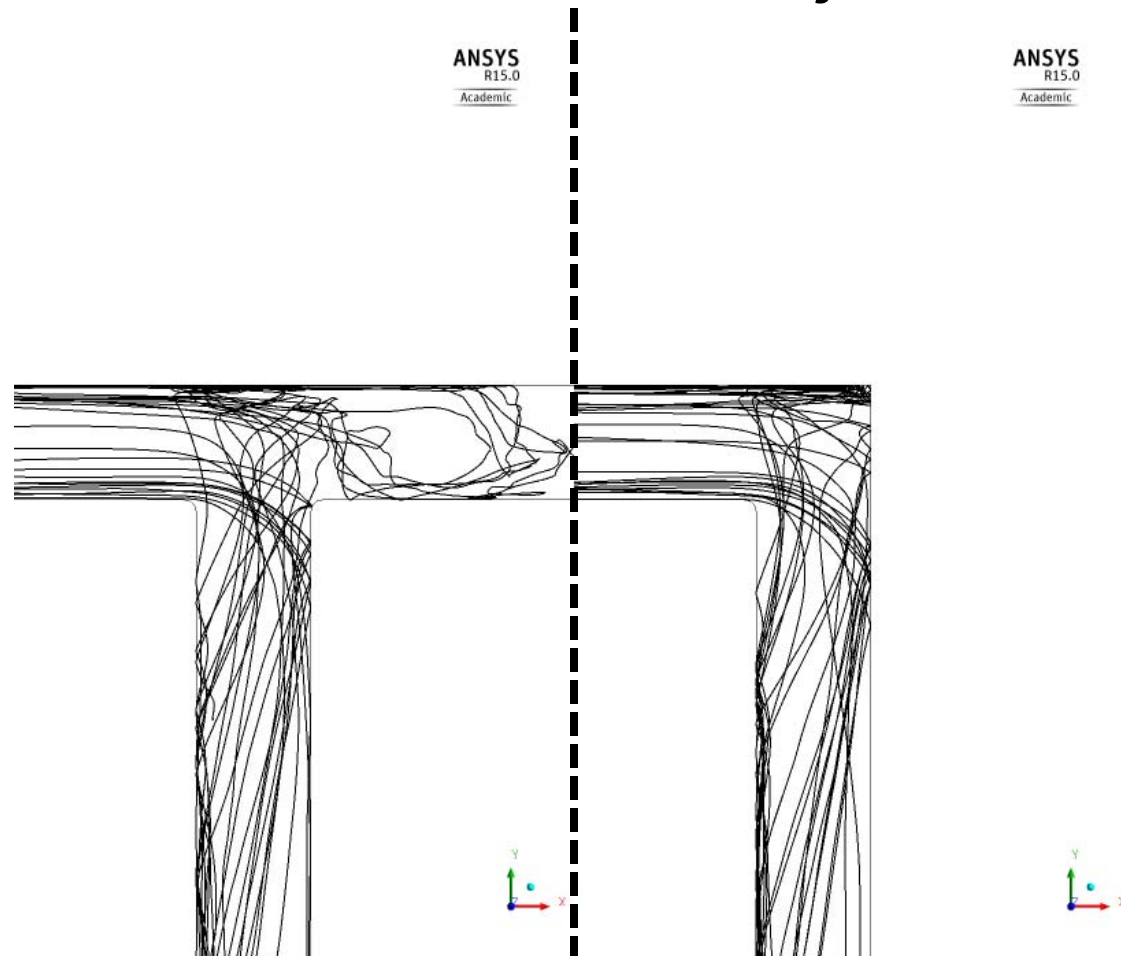
- Steady RSM RANS
- Ducted elbow and plugged T-junction
- Fully turbulent inlet
- Particles are introduced at inlet
- Dilute particle concentration
- Tulsa angle dependent erosion model

|                     |                      |
|---------------------|----------------------|
| Particle diameter   | $1.6 \times 10^{-3}$ |
| Density ratio       | 2.0                  |
| Stokes number       | 4.6                  |
| Volume fraction     | $1.0 \times 10^{-6}$ |
| Number of particles | $7.0 \times 10^5$    |



# RANS RSTM Model

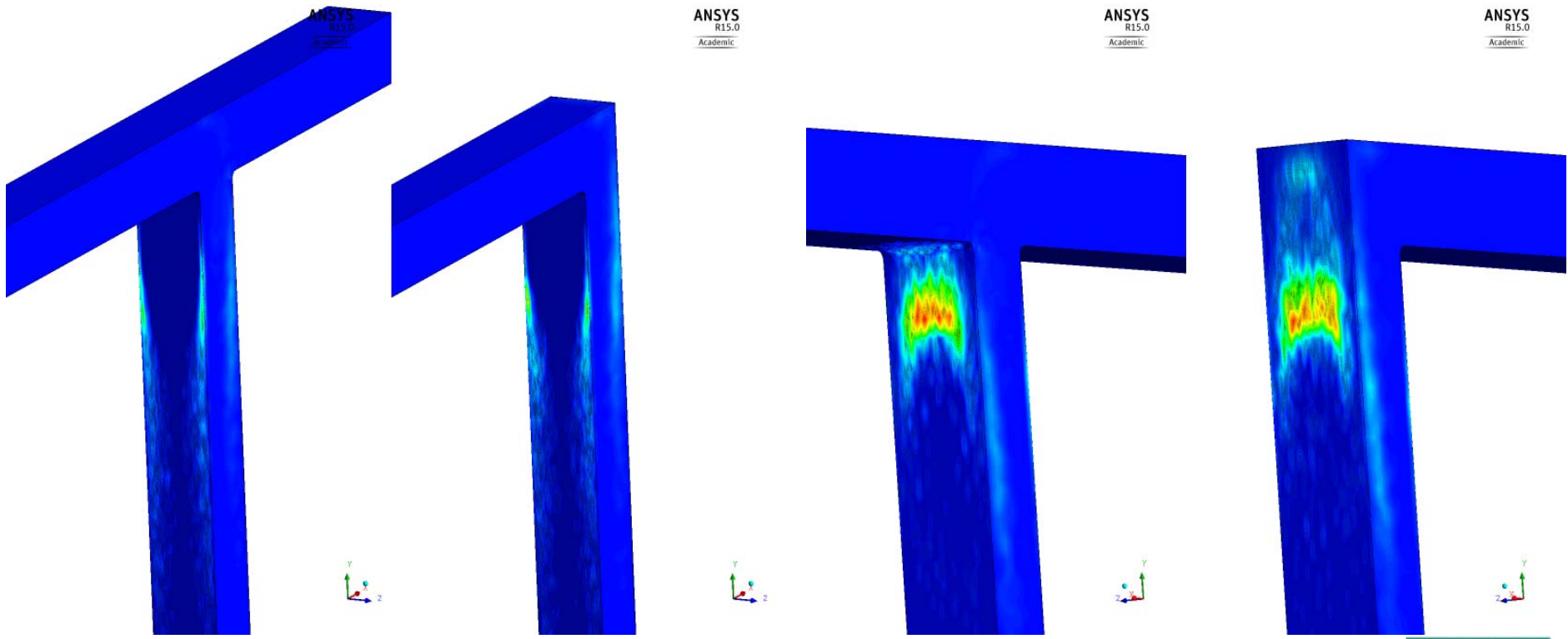
## Predicted Particles Trajectories





# RANS RSM Model

## Predicted Erosion Patterns



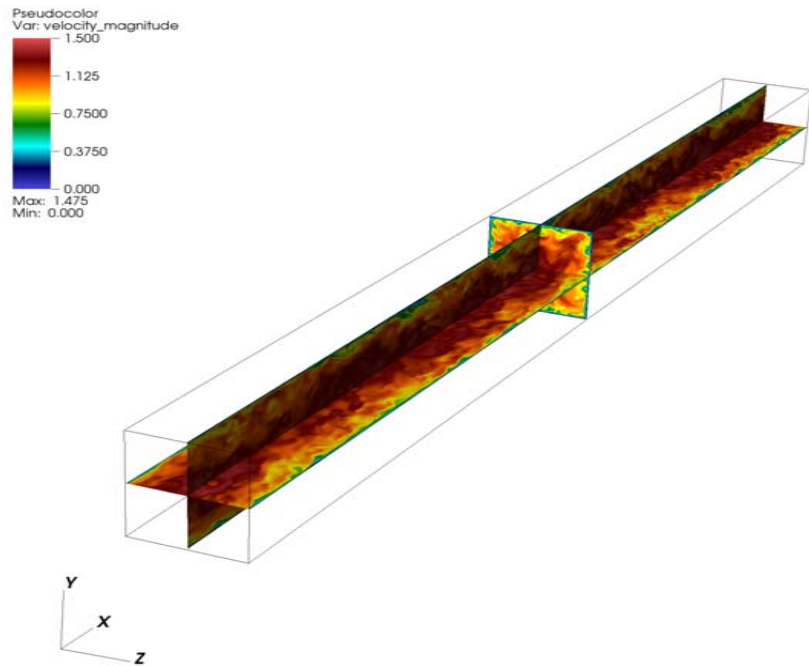
# DNS Duct

- Simulation started with a laminar profile
- Turbulence was initialized using random noise
- Grid will be refined once steady turbulence is achieved
- Periodic boundary condition

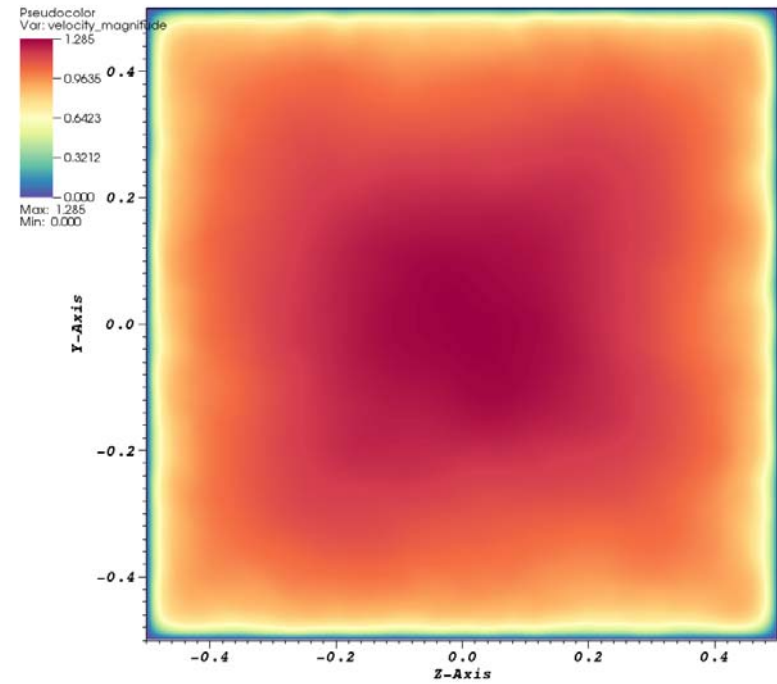
|  |                      |
|--|----------------------|
| Reynolds Number (Re)                   | 11,500               |
| Duct length (L/H)                      | 12.5                 |
| # of elements                          | 202, 176             |
| Polynomial degree                      | 9                    |
| $y^+$ of first nodal point             | 1                    |
| $\Delta y^+_{\max}, \Delta z^+_{\max}$ | 16                   |
| $\Delta x^+_{\max}$                    | 40                   |
| Timestep ( $\Delta t U/H$ )            | $2.5 \times 10^{-4}$ |
| Sample time ( $t U/H$ )                | 27                   |

# DNS Duct

Instantaneous Velocity Pseudocolors

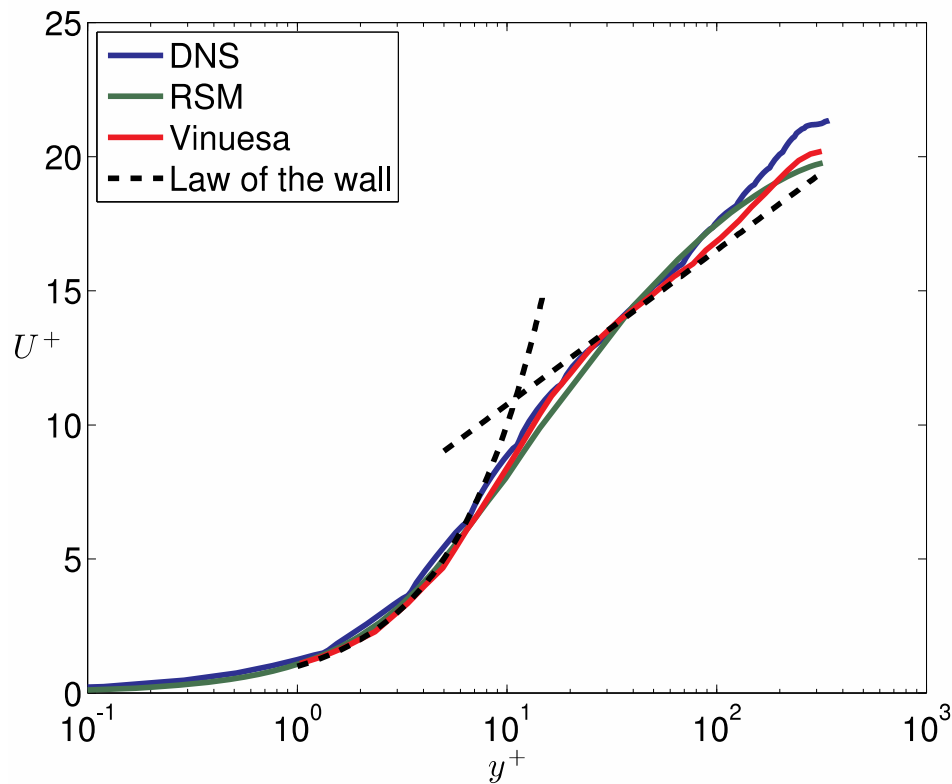


Cross-section Mean Velocity Pseudocolors

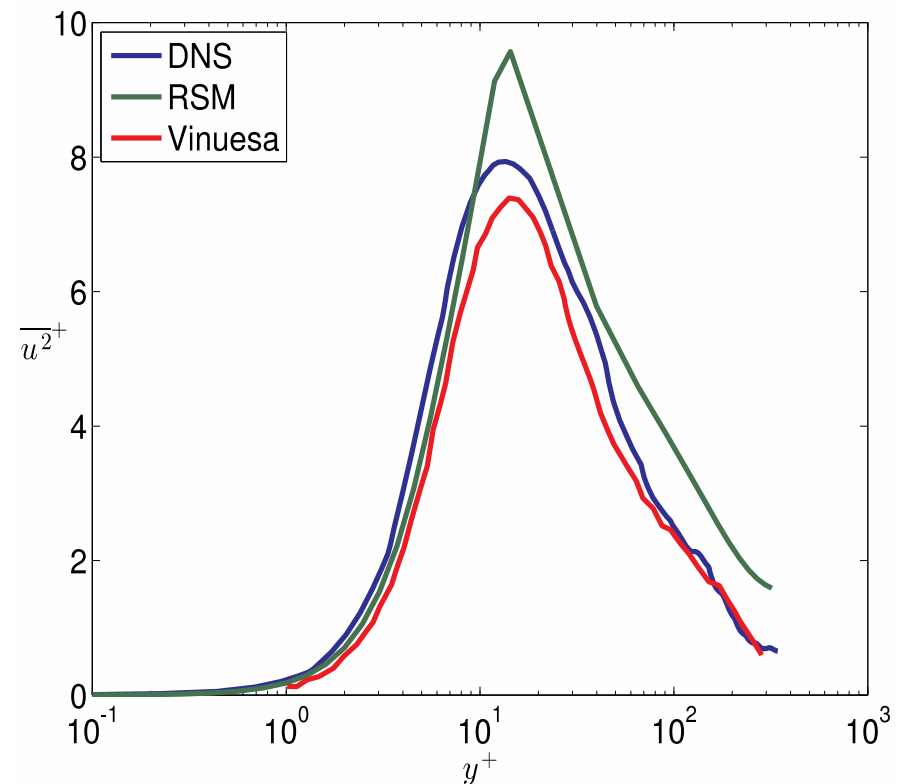


# DNS Duct

Mean Flow

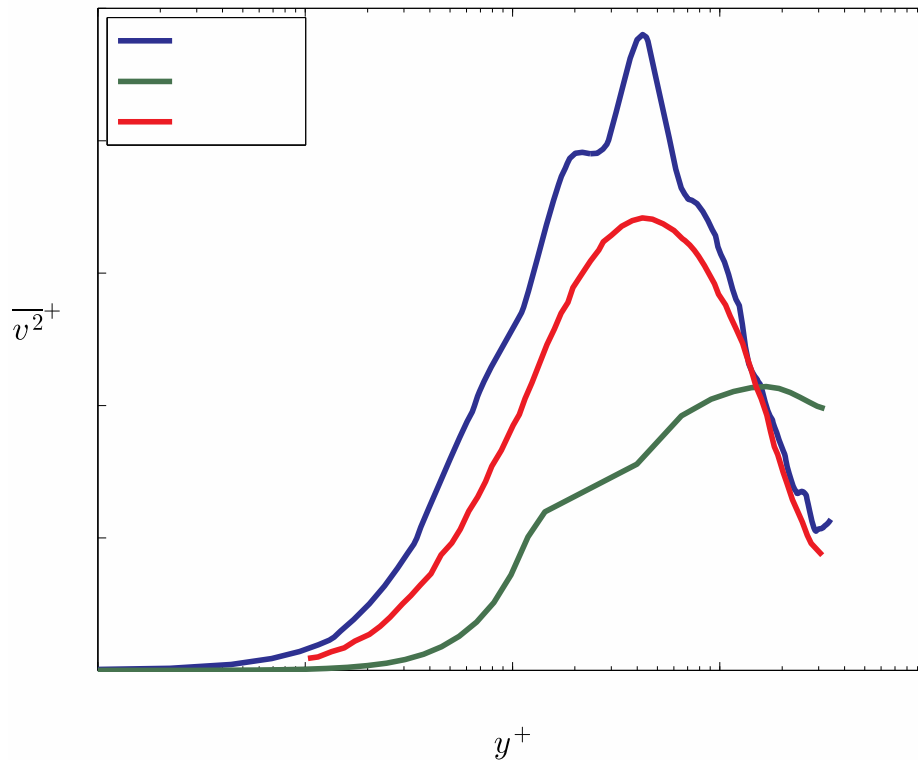


Streamwise turbulent intensities

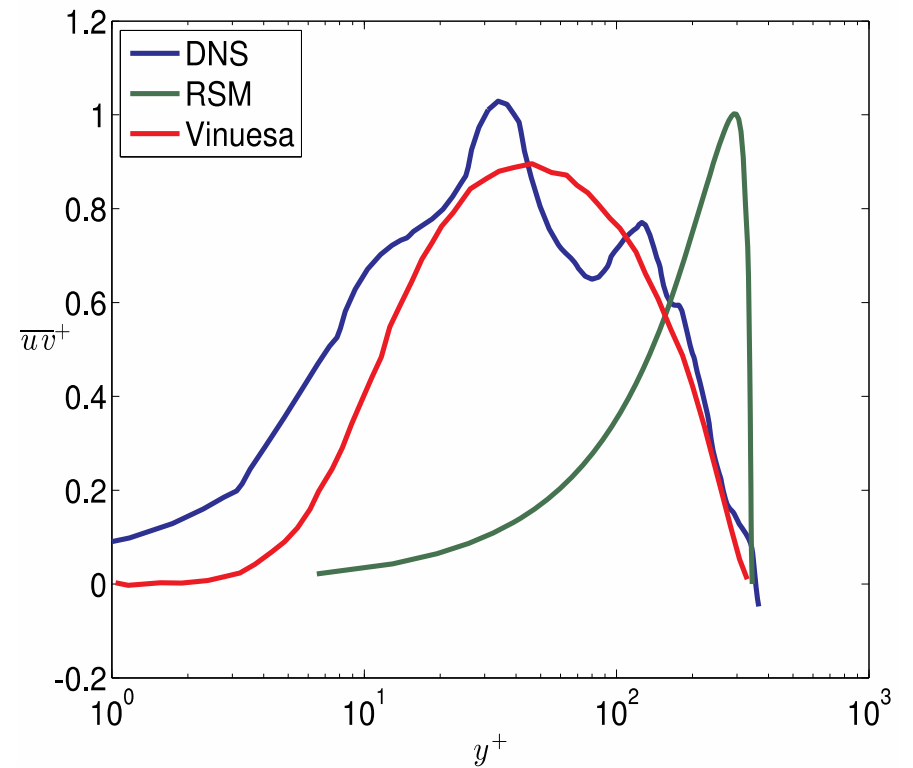


# DNS Duct

Spanwise turbulent intensities

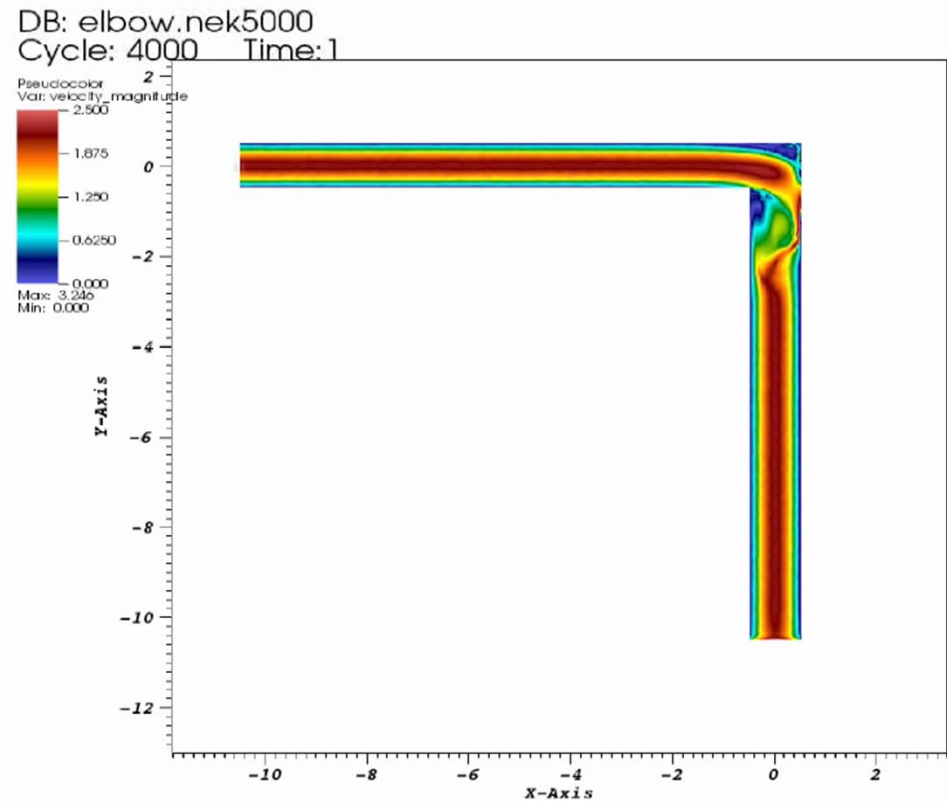


Reynolds shear stress



# Coarse *DNS Elbow*

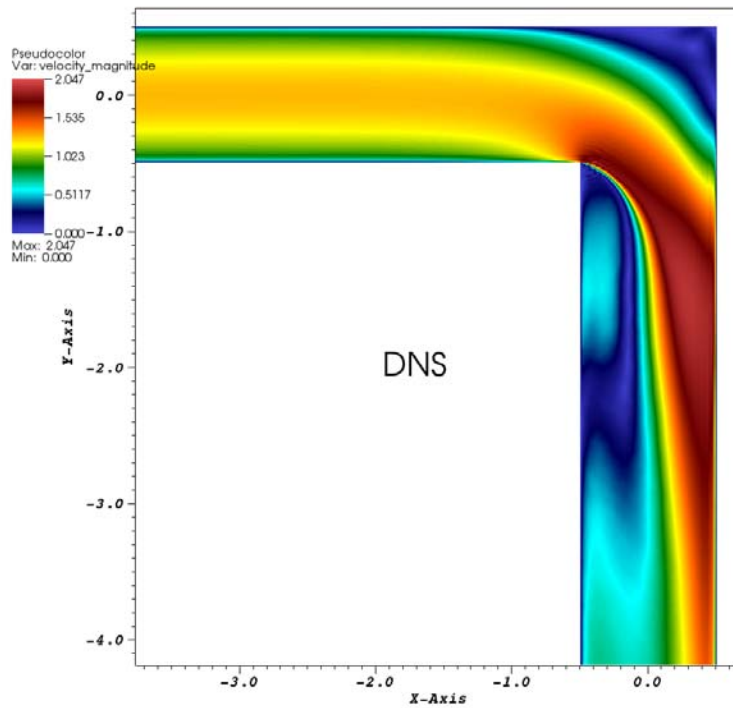
|                              |                      |
|------------------------------|----------------------|
| Reynolds Number (Re)         | 11,500               |
| Entrance length (L/D)        | 10                   |
| Exit length (L/D)            | 10                   |
| # of elements                | 24,768               |
| Polynomial number            | 8                    |
| Total grid points            | $12.68 \times 10^6$  |
| Timestep ( $\Delta t(U/D)$ ) | $2.5 \times 10^{-4}$ |
| Sample time( $t(U/D)$ )      | 185                  |



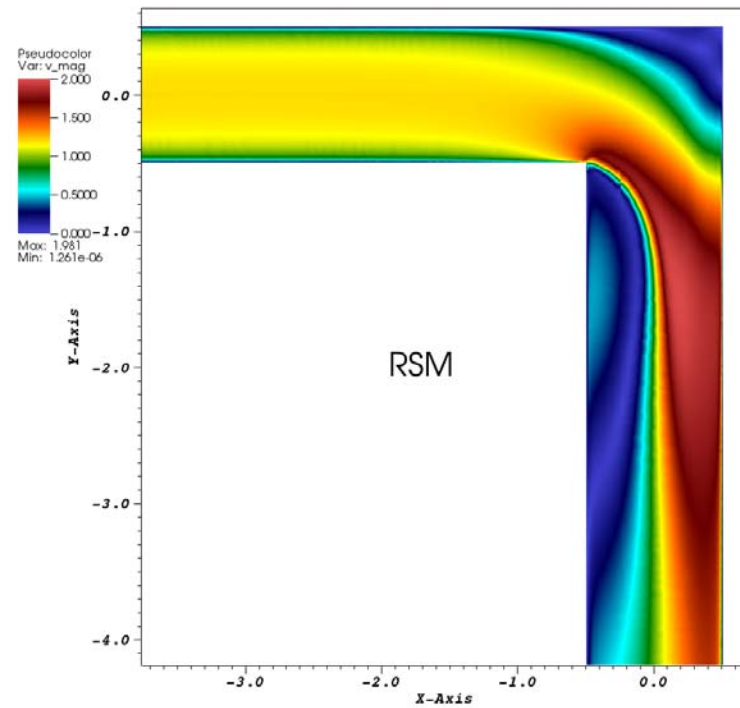
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# Coarse *DNS Elbow*

## Velocity Contours Mid-plane



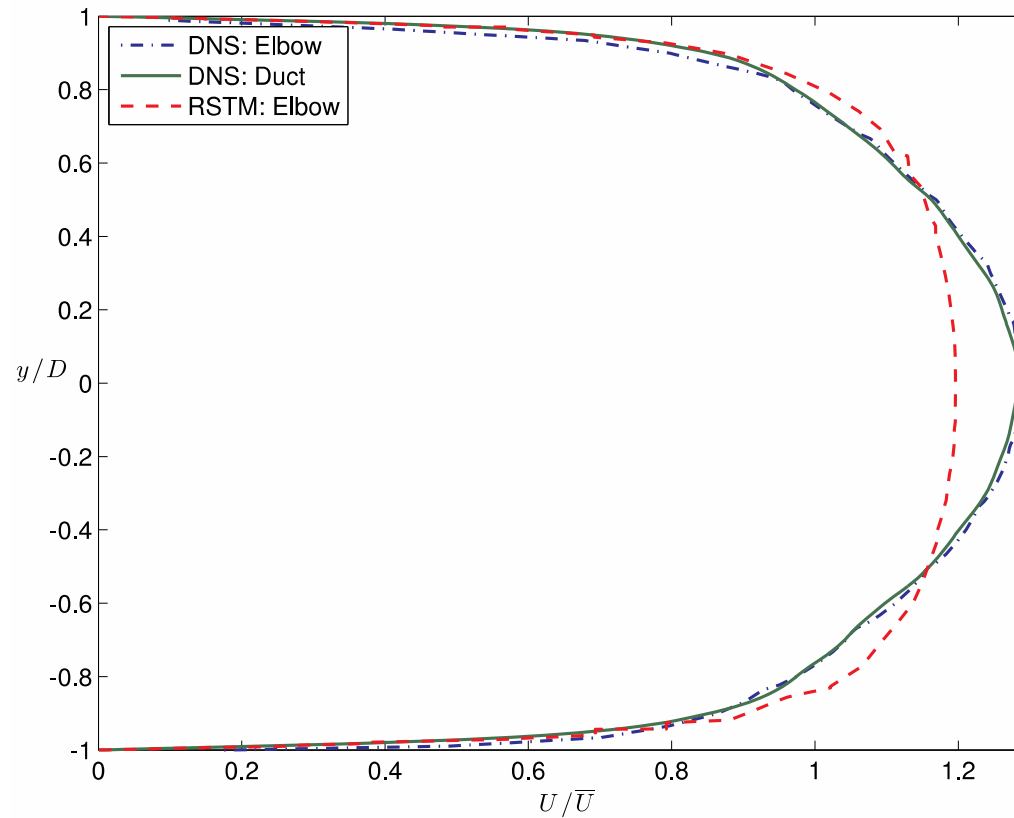
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# Coarse *DNS Elbow*

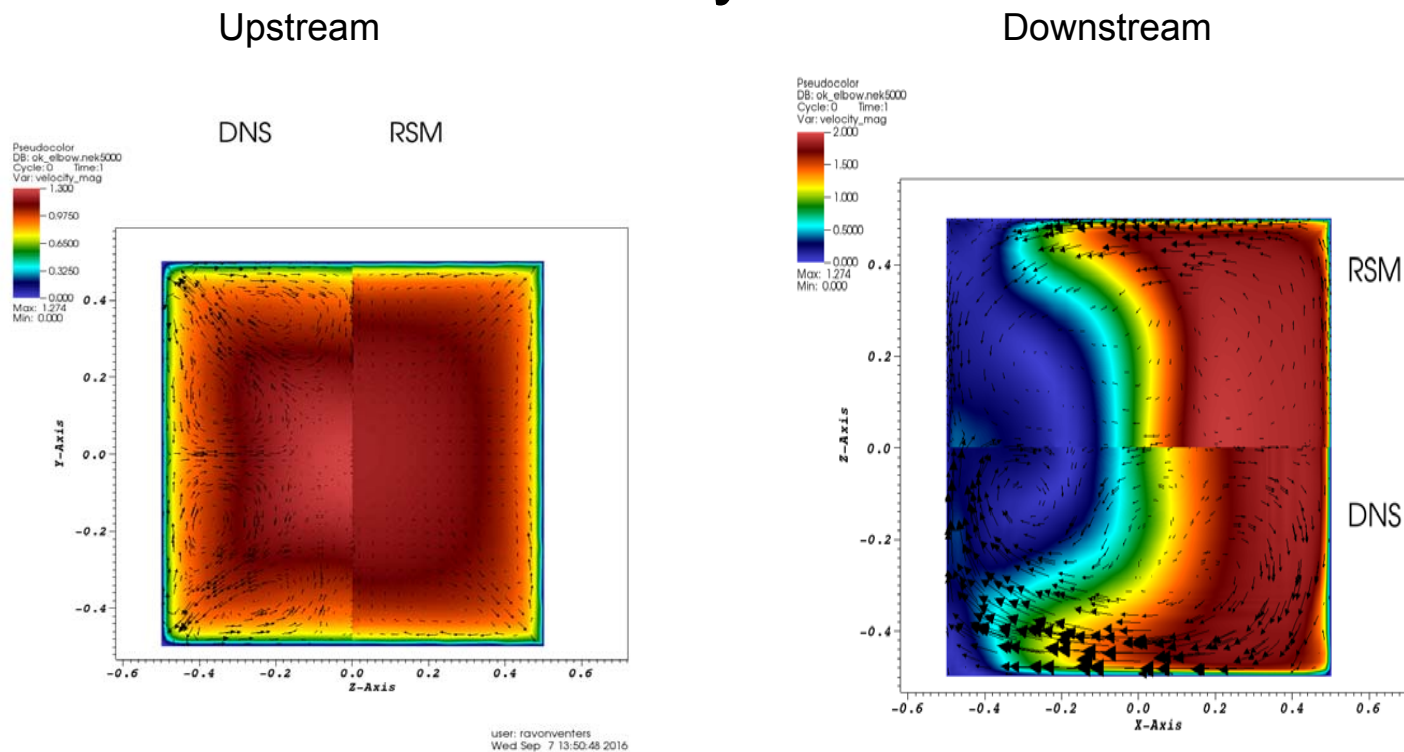
Mean velocity profile





# Coarse *DNS Elbow*

Streamwise velocity overlaid with in-plane velocity vectors



# Future Work

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- In the process of performing one-way coupled DNS in an elbow
- Complete comparison of RANS, DNS, and experimental results
- Validation of the two-way coupled model